Q12 QUIZ CONTEST AND THE GEOMETRIC DISTRIBUTION Statistics for Business, 2019 (Prof.: Josemari Sarasola)

Starting on June 2018, Q12 has become a popular quiz contest in Spain. The program is cast via Android-iOS only for mobile phones, everyday at 22:00. Around 100.000 people take part everyday in the contest. The goal is to answer correctly 12 quiz questions with 3 choices about general culture and also more specific topics. Players are removed from the day's contest when they give a wrong answer for the first time. Players remaining after the 12th question share a 500 euros prize. Questions are easy at the beginning and become more and more difficult; at the end questions are killer: people answer them randomly as they have no idea about it.

Let's suppose all questions are killer. How many players on average remain until the last question and get the prize? And what if questions are easier?



Killer questions: p(right)=1/3, as answers are random

Easier questions: p(right answer)=0.6

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No.players remain		00009	36000	21600	12960	9222	4665.6	2799.4	1679.7	1007.9	604.8	362.9	217.8
Cum.prob.		0.40	0.64	0.784	0.8704	0.922240	0.953344	0.972006	0.983203	0.989921	0.993952	0.996371	0.997822
No.Q. Probability of being removed		0.40	0.24	0.144	0.0864	0.05184	0.031104	0.018662	0.011197	0.006718	0.004031	0.002419	0.001451
No.Q.		1	2	3	4	2	9	2	∞	6	10	11	12
No.players remaining	100.000	33333.3	11111.1	3703.7	1234.6	411.6	137.3	45.9	15.4	5.2	1.8	0.7	0.3
Cum.prob.	1	0.666667	0.888889	0.962963	0.987654	0.995884	0.998627	0.999541	0.999846	0.999948	0.999982	0.999993	0.999997
No.Q. Probability of being removed Cu	1	2999990	0.222222	0.074074	0.024691	0.008230	0.002743	0.000914	0.000305	0.000102	0.000034	0.000011	0.000004
\sim			2	33		25	9				10	11	12

Number of questions correctly answered before first fail with killer questions: X

Number of questions correctly answered before first fail with easier questions: Y

10.3

0.999897

0.000068

0.9999938

0.000041

0.999829

17.1

0.999716

6.2

78.5 47.2 28.4

0.998693 0.999215 0.999528

0.000871 0.000522 0.000313 0.000188 0.000113

13 14 15 16 17 17 19 20 20

3.8

Generally,